

VELOCITY VS TIME GRAPH PHYSICS

UNDERSTANDING VELOCITY VS TIME GRAPHS IN PHYSICS

VELOCITY VS TIME GRAPH PHYSICS PROVIDES A POWERFUL VISUAL TOOL FOR UNDERSTANDING THE MOTION OF OBJECTS. THESE GRAPHS, OFTEN REFERRED TO AS V-T GRAPHS, ARE FUNDAMENTAL TO KINEMATICS, ALLOWING US TO ANALYZE HOW AN OBJECT'S SPEED AND DIRECTION CHANGE OVER A PERIOD. BY EXAMINING THE SLOPE, AREA, AND OVERALL SHAPE OF A VELOCITY-TIME GRAPH, WE CAN GLEAN CRUCIAL INFORMATION ABOUT AN OBJECT'S ACCELERATION, DISPLACEMENT, AND EVEN ITS INSTANTANEOUS VELOCITY AT ANY GIVEN MOMENT. THIS ARTICLE WILL DELVE DEEP INTO THE INTRICACIES OF VELOCITY VS TIME GRAPHS, BREAKING DOWN THEIR COMPONENTS, EXPLORING DIFFERENT SCENARIOS, AND HIGHLIGHTING THEIR SIGNIFICANCE IN COMPREHENDING THE PRINCIPLES OF MOTION. WE'LL COVER EVERYTHING FROM DEFINING VELOCITY AND TIME AXES TO INTERPRETING CONSTANT VELOCITY, ACCELERATION, AND EVEN DECELERATION.

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WHAT IS A VELOCITY VS TIME GRAPH?

A VELOCITY VS TIME GRAPH, IN THE REALM OF PHYSICS, IS A GRAPHICAL REPRESENTATION THAT PLOTS AN OBJECT'S VELOCITY ON THE VERTICAL (Y) AXIS AGAINST TIME ON THE HORIZONTAL (X) AXIS. THIS SIMPLE YET PROFOUND VISUAL AID ALLOWS US TO SEE, AT A GLANCE, HOW AN OBJECT'S VELOCITY IS CHANGING. VELOCITY ITSELF IS A VECTOR QUANTITY, MEANING IT HAS BOTH MAGNITUDE (SPEED) AND DIRECTION. THEREFORE, THE GRAPH CAN DEPICT CHANGES IN SPEED, CHANGES IN DIRECTION, OR BOTH. UNDERSTANDING THESE GRAPHS IS NOT JUST ABOUT MEMORIZING SHAPES; IT'S ABOUT BUILDING AN INTUITIVE GRASP OF HOW FORCES CAUSE OBJECTS TO MOVE AND CHANGE THEIR MOTION. THEY ARE INDISPENSABLE TOOLS FOR STUDENTS, ENGINEERS, AND SCIENTISTS ALIKE WHEN ANALYZING MOTION.

THE IMPORTANCE OF VELOCITY VS TIME GRAPHS

THE IMPORTANCE OF VELOCITY VS TIME GRAPHS CANNOT BE OVERSTATED IN PHYSICS EDUCATION AND APPLICATION. THEY BRIDGE THE GAP BETWEEN ABSTRACT MATHEMATICAL EQUATIONS AND THE TANGIBLE WORLD OF MOVING OBJECTS. IMAGINE TRYING TO DESCRIBE A CAR ACCELERATING, THEN CRUISING, THEN BRAKING SOLELY WITH WORDS – IT WOULD BE CUMBERSOME AND PRONE TO MISINTERPRETATION. A V-T GRAPH, HOWEVER, PRESENTS THIS ENTIRE JOURNEY IN A CLEAR, CONCISE, AND EASILY DIGESTIBLE FORMAT. THEY ARE ESSENTIAL FOR SOLVING PROBLEMS RELATED TO MOTION, PREDICTING FUTURE POSITIONS, AND UNDERSTANDING THE UNDERLYING PHYSICAL PRINCIPLES GOVERNING MOVEMENT.

THE ANATOMY OF A VELOCITY VS TIME GRAPH

BEFORE WE CAN INTERPRET THESE GRAPHS EFFECTIVELY, IT'S CRUCIAL TO UNDERSTAND THEIR FUNDAMENTAL COMPONENTS. EACH AXIS, THE ORIGIN, AND THE PLOTTED LINE ALL CARRY SPECIFIC MEANING THAT CONTRIBUTES TO OUR OVERALL UNDERSTANDING OF THE OBJECT'S MOTION. THINK OF IT LIKE LEARNING THE ALPHABET BEFORE YOU CAN READ A BOOK; MASTERING THESE BASIC ELEMENTS IS THE FIRST STEP TO UNLOCKING THE SECRETS HELD WITHIN THE GRAPH.

THE VERTICAL AXIS: VELOCITY

THE VERTICAL AXIS, CONVENTIONALLY LABELED 'V' OR 'VELOCITY', REPRESENTS THE OBJECT'S VELOCITY AT ANY GIVEN POINT IN TIME. SINCE VELOCITY IS A VECTOR, THIS AXIS CAN DISPLAY BOTH POSITIVE AND NEGATIVE VALUES. A POSITIVE VELOCITY TYPICALLY INDICATES MOTION IN ONE DIRECTION (E.G., TO THE RIGHT OR UPWARDS), WHILE A NEGATIVE VELOCITY SIGNIFIES MOTION IN THE OPPOSITE DIRECTION. THE UNITS FOR VELOCITY ARE USUALLY METERS PER SECOND (M/S), BUT COULD ALSO BE

KILOMETERS PER HOUR (KM/H) OR MILES PER HOUR (MPH), DEPENDING ON THE CONTEXT. THE MAGNITUDE OF THE VELOCITY READING ON THE Y-AXIS CORRESPONDS TO THE OBJECT'S SPEED, WHILE THE SIGN TELLS US ITS DIRECTION.

THE HORIZONTAL AXIS: TIME

THE HORIZONTAL AXIS, LABELED 'T' OR 'TIME', REPRESENTS THE DURATION OVER WHICH THE MOTION IS BEING OBSERVED. TIME ALWAYS MOVES FORWARD, SO THIS AXIS WILL GENERALLY INCREASE FROM LEFT TO RIGHT, STARTING FROM ZERO AT THE ORIGIN. THE UNITS FOR TIME ARE TYPICALLY SECONDS (S), BUT COULD ALSO BE MINUTES OR HOURS. THE INTERVAL ALONG THE TIME AXIS REPRESENTS THE PERIOD DURING WHICH WE ARE ANALYZING THE OBJECT'S VELOCITY. EACH POINT ON THE GRAPH CORRESPONDS TO A SPECIFIC INSTANT IN TIME AND THE OBJECT'S VELOCITY AT THAT EXACT MOMENT.

THE ORIGIN AND AXES INTERSECTION

THE ORIGIN, WHERE THE VELOCITY AND TIME AXES INTERSECT, REPRESENTS THE STATE OF MOTION AT TIME $t=0$. AT THIS POINT, THE VELOCITY OF THE OBJECT IS ALSO ZERO, MEANING IT IS AT REST OR HAS ZERO VELOCITY AT THE START OF THE OBSERVATION. IF THE GRAPH DOES NOT START AT THE ORIGIN ON THE TIME AXIS, IT IMPLIES THAT THE OBSERVATION PERIOD BEGINS AT A LATER TIME. SIMILARLY, IF THE VELOCITY AT $t=0$ IS NOT ZERO, THE OBJECT ALREADY HAS AN INITIAL VELOCITY WHEN OUR OBSERVATION BEGINS.

INTERPRETING THE SLOPE: THE KEY TO ACCELERATION

ONE OF THE MOST INSIGHTFUL ASPECTS OF A VELOCITY VS TIME GRAPH IS ITS SLOPE. THE SLOPE OF A V-T GRAPH DIRECTLY REPRESENTS THE OBJECT'S ACCELERATION. ACCELERATION IS DEFINED AS THE RATE OF CHANGE OF VELOCITY. THEREFORE, HOW STEEP THE VELOCITY IS CHANGING WITH RESPECT TO TIME TELLS US HOW RAPIDLY THE OBJECT IS ACCELERATING OR DECELERATING. UNDERSTANDING THIS RELATIONSHIP IS PARAMOUNT TO DECIPHERING THE DYNAMICS OF MOTION.

POSITIVE SLOPE: ACCELERATION

A POSITIVE SLOPE ON A VELOCITY VS TIME GRAPH INDICATES THAT THE OBJECT IS ACCELERATING. THIS MEANS ITS VELOCITY IS INCREASING OVER TIME. THE STEEPER THE POSITIVE SLOPE, THE GREATER THE ACCELERATION. IMAGINE PUSHING DOWN ON THE ACCELERATOR PEDAL OF A CAR; YOUR SPEED INCREASES RAPIDLY, RESULTING IN A STEEP UPWARD SLANT ON THE V-T GRAPH. THIS POSITIVE ACCELERATION IS OFTEN SEEN IN SITUATIONS WHERE A NET FORCE IS ACTING ON THE OBJECT IN THE DIRECTION OF ITS MOTION.

NEGATIVE SLOPE: DECELERATION

CONVERSELY, A NEGATIVE SLOPE ON A VELOCITY VS TIME GRAPH SIGNIFIES DECELERATION, ALSO KNOWN AS NEGATIVE ACCELERATION. THIS OCCURS WHEN AN OBJECT'S VELOCITY IS DECREASING OVER TIME. A COMMON EXAMPLE IS APPLYING THE BRAKES ON A VEHICLE. THE SPEED REDUCES, AND THE GRAPH WILL SHOW A DOWNWARD SLANT. THIS NEGATIVE ACCELERATION MEANS THE OBJECT IS SLOWING DOWN. IT CAN BE CAUSED BY A NET FORCE ACTING IN THE DIRECTION OPPOSITE TO THE OBJECT'S MOTION.

ZERO SLOPE: CONSTANT VELOCITY

WHEN THE VELOCITY VS TIME GRAPH IS A HORIZONTAL LINE, IT MEANS THE SLOPE IS ZERO. THIS CORRESPONDS TO AN OBJECT MOVING WITH CONSTANT VELOCITY. IN THIS SCENARIO, THE VELOCITY IS NEITHER INCREASING NOR DECREASING, AND THEREFORE, THE ACCELERATION IS ZERO. THE OBJECT IS EITHER AT REST (IF THE LINE IS ON THE TIME AXIS, MEANING $v=0$) OR MOVING AT A STEADY SPEED IN A CONSTANT DIRECTION. THIS REPRESENTS A STATE OF ZERO NET FORCE ACTING ON THE OBJECT, ACCORDING TO NEWTON'S FIRST LAW OF MOTION.

UNDERSTANDING DISPLACEMENT FROM THE AREA UNDER THE CURVE

BEYOND THE SLOPE, THE AREA ENCLOSED BY THE VELOCITY VS TIME GRAPH AND THE TIME AXIS PROVIDES ANOTHER CRITICAL PIECE OF INFORMATION: THE OBJECT'S DISPLACEMENT. DISPLACEMENT IS THE CHANGE IN AN OBJECT'S POSITION, INCLUDING ITS DIRECTION. CALCULATING THIS AREA ALLOWS US TO DETERMINE HOW FAR AN OBJECT HAS MOVED DURING A SPECIFIC TIME INTERVAL. THIS IS PARTICULARLY USEFUL WHEN DEALING WITH NON-CONSTANT ACCELERATION.

AREA OF RECTANGLES: CONSTANT VELOCITY

FOR A SECTION OF THE GRAPH REPRESENTING CONSTANT VELOCITY (A HORIZONTAL LINE), THE AREA UNDER THE CURVE FORMS A RECTANGLE. THE AREA OF THIS RECTANGLE IS SIMPLY THE VELOCITY MULTIPLIED BY THE TIME INTERVAL. THIS IS CONSISTENT WITH THE EQUATION OF MOTION FOR CONSTANT VELOCITY: $\text{DISPLACEMENT} = \text{VELOCITY} \times \text{TIME}$. SO, IF AN OBJECT TRAVELS AT 5 m/s FOR 10 SECONDS, THE AREA UNDER THE GRAPH WOULD BE $5 \text{ m/s} \times 10 \text{ s} = 50 \text{ METERS}$, REPRESENTING ITS DISPLACEMENT.

AREA OF TRIANGLES: CONSTANT ACCELERATION

WHEN DEALING WITH CONSTANT ACCELERATION, THE SECTION OF THE VELOCITY VS TIME GRAPH IS A STRAIGHT LINE WITH A NON-ZERO SLOPE, FORMING A TRIANGLE OR A TRAPEZOID WITH THE TIME AXIS. THE AREA OF A TRIANGLE IS GIVEN BY $\frac{1}{2} \times \text{BASE} \times \text{HEIGHT}$. IN THIS CONTEXT, THE BASE IS THE TIME INTERVAL, AND THE HEIGHT IS THE CHANGE IN VELOCITY DURING THAT INTERVAL. THE AREA OF A TRAPEZOID IS $\frac{1}{2} \times (\text{SUM OF PARALLEL SIDES}) \times \text{HEIGHT}$. THESE CALCULATIONS ALLOW US TO DETERMINE THE DISPLACEMENT EVEN WHEN VELOCITY IS CHANGING UNIFORMLY.

AREA OF COMPLEX SHAPES: VARIABLE ACCELERATION

FOR SECTIONS OF THE GRAPH WITH A CURVED LINE, REPRESENTING VARIABLE ACCELERATION, CALCULATING THE EXACT AREA REQUIRES MORE ADVANCED CALCULUS TECHNIQUES, SPECIFICALLY INTEGRATION. HOWEVER, FOR INTRODUCTORY PHYSICS, ONE CAN OFTEN APPROXIMATE THE AREA BY DIVIDING IT INTO SMALLER SHAPES LIKE RECTANGLES AND TRIANGLES OR BY USING NUMERICAL METHODS. THE PRINCIPLE REMAINS THE SAME: THE AREA UNDER THE V-T CURVE REPRESENTS THE DISPLACEMENT.

COMMON SCENARIOS ON A VELOCITY VS TIME GRAPH

VELOCITY VS TIME GRAPHS ARE USED TO ILLUSTRATE A WIDE VARIETY OF MOTION SCENARIOS. BY RECOGNIZING THE PATTERNS, WE CAN QUICKLY UNDERSTAND THE STORY OF AN OBJECT'S MOVEMENT WITHOUT NEEDING TO PERFORM COMPLEX CALCULATIONS. LET'S EXPLORE SOME OF THE MOST FREQUENTLY ENCOUNTERED SITUATIONS.

CONSTANT VELOCITY MOTION

AS DISCUSSED, CONSTANT VELOCITY MOTION IS DEPICTED BY A HORIZONTAL LINE ON THE VELOCITY VS TIME GRAPH. THE VELOCITY VALUE REMAINS THE SAME THROUGHOUT THE OBSERVED TIME INTERVAL, MEANING THE ACCELERATION IS ZERO. THIS COULD BE AN OBJECT MOVING AT A STEADY 10 m/s TO THE RIGHT OR A CAR CRUISING ON A HIGHWAY AT A CONSTANT SPEED.

CONSTANT ACCELERATION MOTION

THIS IS A VERY COMMON SCENARIO IN PHYSICS PROBLEMS. A CONSTANT ACCELERATION IS REPRESENTED BY A STRAIGHT, SLOPED LINE ON THE VELOCITY VS TIME GRAPH.

- IF THE LINE SLOPES UPWARDS, THE OBJECT IS SPEEDING UP WITH A CONSTANT POSITIVE ACCELERATION.
- IF THE LINE SLOPES DOWNWARDS, THE OBJECT IS SLOWING DOWN WITH A CONSTANT NEGATIVE ACCELERATION (DECELERATION).
- THE STEEPER THE SLOPE, THE GREATER THE MAGNITUDE OF THE CONSTANT ACCELERATION.

VARIABLE ACCELERATION

WHEN AN OBJECT'S ACCELERATION IS NOT CONSTANT, THE VELOCITY VS TIME GRAPH WILL SHOW A CURVED LINE. THIS MEANS THE RATE AT WHICH THE VELOCITY IS CHANGING IS ITSELF CHANGING. FOR INSTANCE, THE ACCELERATION MIGHT INCREASE OR DECREASE OVER TIME, OR IT MIGHT FLUCTUATE. ANALYZING SUCH GRAPHS OFTEN REQUIRES BREAKING DOWN THE CURVE INTO SMALLER, MORE MANAGEABLE SEGMENTS OR USING CALCULUS FOR PRECISE CALCULATIONS.

DECELERATION AND BRAKING

DECELERATION, OR SLOWING DOWN, IS VISUALIZED AS A DOWNWARD SLOPING LINE ON THE VELOCITY VS TIME GRAPH. WHEN A CAR BRAKES, ITS VELOCITY DECREASES OVER TIME, LEADING TO THIS CHARACTERISTIC NEGATIVE SLOPE. IF THE BRAKING IS UNIFORM (CONSTANT DECELERATION), THE LINE WILL BE STRAIGHT. IF THE BRAKING FORCE VARIES (E.G., DIFFERENT PRESSURE ON THE BRAKE PEDAL), THE CURVE MIGHT BE NON-LINEAR.

ANALYZING COMPLEX MOTION WITH VELOCITY VS TIME GRAPHS

MANY REAL-WORLD SCENARIOS INVOLVE COMBINATIONS OF DIFFERENT TYPES OF MOTION. A VELOCITY VS TIME GRAPH IS AN EXCELLENT TOOL FOR DISSECTING THESE COMPLEX MOVEMENTS INTO SIMPLER, UNDERSTANDABLE PARTS. FOR EXAMPLE, CONSIDER A JOURNEY THAT INVOLVES STARTING FROM REST, ACCELERATING TO A CRUISING SPEED, AND THEN BRAKING TO A STOP. THIS WOULD BE REPRESENTED BY A SERIES OF DISTINCT SEGMENTS ON THE GRAPH: AN INITIAL UPWARD SLOPE, A HORIZONTAL LINE, AND A FINAL DOWNWARD SLOPE.

COMBINING SEGMENTS

BY ANALYZING EACH SEGMENT OF THE GRAPH SEPARATELY, WE CAN UNDERSTAND THE OBJECT'S BEHAVIOR DURING DIFFERENT PHASES OF ITS MOTION. WE CAN DETERMINE THE ACCELERATION DURING EACH PHASE BY LOOKING AT THE SLOPE AND THE TOTAL DISPLACEMENT DURING EACH PHASE BY CALCULATING THE AREA UNDER THAT SPECIFIC SEGMENT. THIS ALLOWS FOR A COMPREHENSIVE UNDERSTANDING OF THE ENTIRE MOTION.

PRACTICAL APPLICATIONS

THE APPLICATIONS OF VELOCITY VS TIME GRAPHS EXTEND FAR BEYOND THEORETICAL PHYSICS PROBLEMS. THEY ARE USED IN:

- ENGINEERING: DESIGNING VEHICLES, ANALYZING CRASH TEST DATA, AND UNDERSTANDING THE MOTION OF MACHINERY.
- SPORTS: ANALYZING THE PERFORMANCE OF ATHLETES IN ACTIVITIES LIKE RUNNING, CYCLING, AND RACING.
- ROBOTICS: PROGRAMMING AND CONTROLLING THE MOVEMENT OF ROBOTS.
- AEROSPACE: DESIGNING SPACECRAFT TRAJECTORIES AND UNDERSTANDING SATELLITE MOTION.

THESE GRAPHS PROVIDE AN INTUITIVE AND POWERFUL WAY TO VISUALIZE AND ANALYZE MOTION, MAKING THEM AN INDISPENSABLE TOOL IN NUMEROUS SCIENTIFIC AND TECHNOLOGICAL FIELDS. THEY OFFER A CLEAR PICTURE OF HOW VELOCITY CHANGES, WHICH IS THE ESSENCE OF UNDERSTANDING HOW OBJECTS MOVE AND INTERACT IN THE UNIVERSE.

FAQ

Q: WHAT IS THE PRIMARY INFORMATION CONVEYED BY THE SLOPE OF A VELOCITY VS TIME GRAPH?

A: THE SLOPE OF A VELOCITY VS TIME GRAPH DIRECTLY REPRESENTS THE OBJECT'S ACCELERATION. A POSITIVE SLOPE INDICATES ACCELERATION (SPEEDING UP), A NEGATIVE SLOPE INDICATES DECELERATION (SLOWING DOWN), AND A ZERO SLOPE SIGNIFIES CONSTANT VELOCITY (NO ACCELERATION).

Q: HOW CAN DISPLACEMENT BE DETERMINED FROM A VELOCITY VS TIME GRAPH?

A: THE DISPLACEMENT OF AN OBJECT CAN BE FOUND BY CALCULATING THE AREA UNDER THE VELOCITY VS TIME GRAPH BETWEEN THE DESIRED TIME INTERVALS. FOR CONSTANT VELOCITY, THIS IS A RECTANGLE; FOR CONSTANT ACCELERATION, IT'S A TRIANGLE OR TRAPEZOID; AND FOR VARIABLE ACCELERATION, IT INVOLVES MORE COMPLEX AREA CALCULATIONS.

Q: WHAT DOES IT MEAN IF A VELOCITY VS TIME GRAPH IS A HORIZONTAL LINE?

A: A HORIZONTAL LINE ON A VELOCITY VS TIME GRAPH SIGNIFIES THAT THE OBJECT IS MOVING WITH CONSTANT VELOCITY. ITS SPEED AND DIRECTION ARE NOT CHANGING, MEANING ITS ACCELERATION IS ZERO.

Q: CAN A VELOCITY VS TIME GRAPH SHOW AN OBJECT CHANGING DIRECTION?

A: YES, A VELOCITY VS TIME GRAPH CAN SHOW AN OBJECT CHANGING DIRECTION. THIS OCCURS WHEN THE VELOCITY CHANGES SIGN, CROSSING THE TIME AXIS FROM POSITIVE TO NEGATIVE OR VICE VERSA. FOR EXAMPLE, AN OBJECT MOVING FORWARD AND THEN REVERSING WOULD SHOW A VELOCITY THAT STARTS POSITIVE, BECOMES ZERO, AND THEN BECOMES NEGATIVE.

Q: WHAT TYPE OF MOTION IS REPRESENTED BY A CURVED LINE ON A VELOCITY VS TIME GRAPH?

A: A CURVED LINE ON A VELOCITY VS TIME GRAPH INDICATES VARIABLE ACCELERATION. THIS MEANS THE RATE AT WHICH THE OBJECT'S VELOCITY IS CHANGING IS NOT CONSTANT; IT'S EITHER INCREASING OR DECREASING OVER TIME.

Q: HOW IS DECELERATION SPECIFICALLY VISUALIZED ON A VELOCITY VS TIME GRAPH?

A: DECELERATION, OR SLOWING DOWN, IS VISUALIZED AS A DOWNWARD SLOPING LINE ON A VELOCITY VS TIME GRAPH. THE VELOCITY IS DECREASING AS TIME PROGRESSES.

Q: IF AN OBJECT STARTS FROM REST, WHAT WOULD ITS VELOCITY VS TIME GRAPH LOOK LIKE AT THE BEGINNING?

A: IF AN OBJECT STARTS FROM REST, ITS INITIAL VELOCITY IS ZERO. THEREFORE, ITS VELOCITY VS TIME GRAPH WOULD BEGIN AT THE ORIGIN (0,0) ON THE GRAPH, ASSUMING THE OBSERVATION STARTS AT TIME $t=0$.

Q: IS IT POSSIBLE FOR A VELOCITY VS TIME GRAPH TO HAVE SEGMENTS WITH BOTH POSITIVE AND NEGATIVE SLOPES?

A: ABSOLUTELY. A VELOCITY VS TIME GRAPH CAN INDEED HAVE SEGMENTS WITH BOTH POSITIVE AND NEGATIVE SLOPES. THIS REPRESENTS PERIODS WHERE THE OBJECT IS ACCELERATING, FOLLOWED BY PERIODS WHERE IT IS DECELERATING, OR VICE VERSA, WHICH IS COMMON IN MANY REAL-WORLD MOTION SCENARIOS.

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